

Homework 2

1. Sec.1.4: 20, 24, 26.
2. Sec. 1.5: 4
3. Prove that $p \rightarrow (q \wedge r) \equiv (p \rightarrow q) \wedge (p \rightarrow r)$ using identities or truth tables. Then use this equivalence and the rules of inference to show the following premises

$$q \rightarrow (u \wedge t), u \rightarrow p, (p \wedge t) \rightarrow (r \vee s), \neg s$$

imply the conclusion $q \rightarrow r$.

4. Let $S(x) = "x \text{ is in this class}"$, $R(y) = "y \text{ owns a red convertible}"$, $T(z) = "z \text{ has gotten a speeding ticket}"$.
 - a. For each of the statements below, please translate them into propositions using $S(x)$, $R(y)$ and $T(z)$ with quantifiers.
 - (i) Linda, a student in this class, owns a red convertible.
 - (ii) Everyone who owns a red convertible has gotten at least one speeding ticket.
 - (iii) Therefore, someone in this class has gotten a speeding ticket.
 - b. Next, using the rules of inference, show why statement (iii) follows from statements (i) and (ii).

5. Sec. 1.5: 16.